## Grammar and <br> Feature Unification

## Problems with CF Phrase Structure Grammars

- Difficult to capture dependencies between constituents
- the boy runs
- the boys run
-     * the boy run
-     * the boys runs


## Problems with CF Phrase Structure Grammars

- Difficult to capture dependencies between constituents
- the boy opens the door
- *?? the boy opens
- the boy hops
- *?? the boy hops the table


## CF Solution

- exploding the number of rules is one way to provide a solution...

```
S }->\mathrm{ NPsing VPsing
S }->\mathrm{ NPplural VPplural
NP }->\mathrm{ NPsing
NP }->\mathrm{ NPplural
NPsing }->\mathrm{ Detsing Nsing
NPplural }->\mathrm{ Detplural Nplural
VPsing }->\mathrm{ Vintsing
VPplural }->\mathrm{ Vintplural
VPsing }->\mathrm{ Vtrsing NP
VPplural }->\mathrm{ Vtrplural NP
```

| Detsing $\rightarrow$ \{a, this, the $\}$ |
| :--- |
| Detplural $\rightarrow$ \{some, these, the $\}$ |
| Nsing $\rightarrow$ \{boy, girl, $\ldots\}$ |
| Nplural $\rightarrow$ boys, girls, $\ldots\}$ |
| Vintsing $\rightarrow$ \{hops, $\ldots\}$ |
| Vintplural $\rightarrow$ \{hop, $\ldots\}$ |
| Vtrsing $\rightarrow$ \{opens, $\ldots\}$ |
| Vtrplural $\rightarrow$ \{open, ...\} |

## A better solution...

- What we really want to say is that some constituents share properties


## The boy runs

the 'Subject' and the 'Verb' agree in number

- i.e., they share the same value for their number feature


## Phrase structure rules with features

$$
\mathrm{S} \quad \rightarrow \begin{gathered}
\text { NP } \\
+ \text { singular }
\end{gathered} \quad \begin{gathered}
\text { VP } \\
+ \text { singular }
\end{gathered}
$$

$\mathrm{VP} \quad \rightarrow \quad \mathrm{V} \quad$ (NP)
+singular +singular

## Phrase structure rules with features

$$
\mathrm{S} \quad \rightarrow \begin{gathered}
\mathrm{NP} \\
+ \text { plural }
\end{gathered} \quad \begin{gathered}
\mathrm{VP} \\
+ \text { plural }
\end{gathered}
$$

$\underset{+ \text { plural }}{\mathrm{VP}} \rightarrow \underset{\text { +plural }}{\mathrm{V}} \quad(\mathrm{NP})$

## Features $\rightarrow$ Feature structures

Attribute-value matrices (AVMs)
+singular
[number: singular]
+ing-form
[verb: ing-form]
+masc

+ sing
(gender: masc number: sing

Feature structures
Unification

Compatibility
Information

## Phrase structure rules with features

$$
\mathrm{S} \quad \rightarrow \begin{gathered}
\text { NP } \\
+ \text { singular }
\end{gathered} \quad \begin{gathered}
\text { VP } \\
+ \text { singular }
\end{gathered}
$$

$\mathrm{VP} \quad \rightarrow \quad \mathrm{V} \quad$ (NP)
+singular +singular

## Phrase structure rules with features

$$
\mathrm{S} \quad \rightarrow \underset{ }{[\text { number: sing }]} \mathrm{NP} \stackrel{\text { VP }}{\text { [ number: sing] }}
$$

$\mathrm{VP} \rightarrow \mathrm{V} \quad$ (NP)
[ number: sing] [ number: sing ]

## Phrase structure rules with features

$$
\mathrm{S} \quad \rightarrow \underset{[\text { number: } \mathrm{pl}]}{\mathrm{NP}} \quad \begin{gathered}
\mathrm{VP} \\
{[\text { number: } \mathrm{pl}]}
\end{gathered}
$$

$\mathrm{VP} \rightarrow \mathrm{V} \quad$ (NP)
[ number: pl] [ number: pl ]

## Phrase structure rules with features



## Phrase structure rules with features



## Generalised Rules

$$
\mathrm{S} \quad \rightarrow \begin{gathered}
\mathrm{NP} \\
{[\text { number: } \mathrm{x}]}
\end{gathered} \quad \begin{gathered}
\text { VP } \\
{[\text { number: } \mathrm{x}]}
\end{gathered}
$$

## $\mathrm{VP} \quad \rightarrow \quad \mathrm{V} \quad$ (NP)

[ number: x] [ number: x ]

## Example Grammar

| Parameter start symbol is S |  | Rule | \{VP intransitiv\}VP -> Vi. |
| :---: | :---: | :---: | :---: |
| Rule | \{Satz\} |  |  |
|  | S -> NP VP. |  |  |
|  |  | Rule | \{VP transitiv\} |
| Rule | \{NP-Name\} |  | VP -> Vt NP. |
|  | NP -> Name. |  |  |
|  |  | Rule | \{VP transitiv mit PP\} |
| Rule | \{NP\} |  | VP -> Vt NP PP. |
|  | NP -> Det N . |  |  |
|  |  | Rule | \{VP ditransitiv\} |
|  |  |  | VP -> Vt2 NP NP. |
|  |  | Rule | \{VP mit PP-Objekt $\}$ |
|  |  |  | VP -> Vpo PP. |
| PATR-formalism |  |  |  |
|  |  | Rule | \{einfache PP\} |
|  |  |  | PP -> P NP. |

## Example Lexicon

| Iw cried | Iw girl | Iw the |
| :--- | :--- | :--- |
| Ic Vi | Ic N | Ic Det |
|  |  |  |
| Iw saw | Iw student | Iw a |
| Ic Vt | Ic N | Ic Det |
|  |  |  |
| Iw gave | Iw book | Iw in |
| Ic Vt2 | Ic N | Ic P |
|  |  | Iw on |
|  |  | Ic P |

## PATR-formalism

$\square$

## Example Lexicon (with features)

| Iw cried | Iw girl | Iw the |
| :--- | :--- | :--- |
| Ic Vi | Ic N | Ic Det |
|  | If sg |  |
| Iw saw |  | Iw a |
| Ic Vt | Iw student | Ic Det |
|  | Ic N |  |
| Iw gave | If sg | Iw in |
| Ic $\mathrm{Vt2}$ |  | Ic P |
|  | Iw book |  |
| Iw sings | Ic N | Iw on |
| Ic Vi | If sg | Ic P |
| If 3 sg |  |  |
|  | Iw girls |  |
|  | Ic N |  |
|  | If pl |  |
|  | Iw students |  |
|  | Ic N |  |
|  | If pl |  |

## Example Lexicon (with features)



## Example Lexicon (with features)



## Generalised Rules

$$
\mathrm{S} \quad \rightarrow \begin{gathered}
\mathrm{NP} \\
{[\text { number: } \mathrm{x}]}
\end{gathered} \quad \begin{gathered}
\text { VP } \\
{[\text { number: } \mathrm{x}]}
\end{gathered}
$$

## $\mathrm{VP} \quad \rightarrow \quad \mathrm{V} \quad$ (NP)

[ number: x] [ number: x ]

## Feature Representation

- Syntactic tree becomes a more complex structure
- Each node in the tree is in fact a bundle of features
- Particular rules (specified in the grammar) specify what conditions hold on the feature structures
- Usually: local - i.e., conditions hold over a dominating node and its children


## Generalised Rules (PATR formalism)

$$
\begin{aligned}
& \mathrm{S} \quad \rightarrow \quad \mathrm{NP} \\
& <\text { NP number }>=\text { VVP number> }
\end{aligned}
$$

$$
\mathrm{VP} \quad \rightarrow \mathrm{~V} \quad \text { (NP) }
$$

<VP number> = <V number>

Grammar $=\{P S-r u l e s+$ path equations $\}$

## Feature Geometries

- Much of modern linguistics is now to do with bundles of features
- and how these are distributed around syntactic structures
- Some special kinds of features flow along the ‘backbone' provided by the tree structures: head features


# Head features are usually 'passed up' to the dominating node 

$\mathrm{S} \rightarrow \mathrm{NP}$ VP
<NP head num> $=<$ VP head num>
<NP head pers>
= $<V P$ head pers>

# Head features are usually 'passed up' to the dominating node 

```
Rule {VP intransitiv}
VP }->\mathrm{ V:
<VP head> = <V>
<V subcat> = i.
```

$\underset{\substack{\text { Ic } \mathrm{Vi} \\ \text { If } 3 \mathrm{sig}}}{\substack{\text { Iw sings }}} \xrightarrow[{[\text { lex: sings] }}]{[\text { cat: } \mathrm{V}] .}$

Let V be [cat: V ].
Let Vi be V [subcat: i].
[cat: V
subcat: i]

## exercise with the example grammar...

what structure (both tree structure and feature structure) does the grammar produce for:

## "the boys sing"

and what would it do for

> "the boy sing"

## Feature-based Parsing: "the boys sing"

1:


```
S:
[ cat: S
    subj: [ cat: NP
        lex: the
        num: pl ]
        head:
                            [ cat: 
                                lex: boys
        num: pl
        pers: 3 ] ]
    pred: [ cat: VP
        head: [ cat: v
        subcat:i
        lex: sing
        num: pl
        pers: 3 ] ] ]
1 parse found
```


## Final move...

- All information is moved into the feature structure - even the tree structure...
- HPSG
(Head-driven Phrase Structure Grammar)


